THE O.P. GUPTA

ADVANCED MATH CLASSES

Mathematics (Standard & Basic) **Topic - Introduction to Trigonometry**





Max. Marks - 40 Time - 90 Minutes

SECTION A

Followings multiple choice questions are of 1 Mark each (Q01-10). Select the correct option in each one of them.

Q01. If
$$\sin \theta = \frac{3}{5}$$
, then $\cos \theta$ is

(A)
$$\frac{4}{5}$$
 (B) $\frac{5}{4}$

(B)
$$\frac{5}{4}$$

(C)
$$\frac{3}{4}$$

(D)
$$\frac{2}{5}$$

Q02. If
$$\cos A = \frac{12}{13}$$
, then $\tan A =$

(A)
$$\frac{13}{12}$$

(B)
$$\frac{12}{5}$$

(C)
$$\frac{5}{13}$$

(D)
$$\frac{5}{12}$$

Q03. The value of
$$\sec^2 \theta - \tan^2 \theta$$
 is always

$$(C) \pm 1$$

Q04. The value of
$$\tan 45^{\circ} + \cos 60^{\circ} - \sin 30^{\circ}$$
 is

$$(A) -1$$

Q05. The value of
$$\cos 30^{\circ} \times \sec 30^{\circ}$$
 is

$$(A) -1$$

Which of the following is **not** correct? O06.

(A)
$$\sin 90^{\circ} = 1$$

(B)
$$\cos 0^{\circ} = 1$$

(C)
$$\tan 0^{\circ} = 1$$

(D)
$$\cot 30^{\circ} = \sqrt{3}$$

Q07. The value of
$$\frac{1+\tan^2\theta}{1+\cot^2\theta}$$
 is

(B)
$$\sec^2 \theta$$

(C)
$$\sin^2 \theta$$

Q08. If
$$\tan A + \cot A = 2$$
, then the value of $\tan^2 A + \cot^2 A$ is

$$(A) -1$$

Followings are Assertion-Reason based questions (Q09 & 10).

In the following questions, a statement of Assertion (A) is followed by a statement of Reason (R). Choose the correct answer out of the following choices.

- (A) Both **A** and **R** are true and **R** is the correct explanation of **A**.
- (B) Both A and R are true and R is not the correct explanation of A.
- (C) A is true but R is false.
- (D) **A** is false but **R** is true.

Q09. **Assertion** (A): If
$$\sec \theta + \tan \theta = p$$
, then the value of $\sec \theta - \tan \theta$ is $\frac{1}{p}$.

Reason (R): If
$$\sin \phi = \frac{1}{2}$$
, then $\phi = 30^{\circ}$.

Q10. **Assertion (A)**: If
$$\sin \theta + \cos \theta = \frac{3}{2}$$
, then the value of $\sin^3 \theta + \cos^3 \theta = \frac{9}{16}$.

Reason (R): In a right angled triangle with an acute angle
$$\theta$$
, we have $\sin^2 \theta + \cos^2 \theta = \pm \frac{1}{2}$.

 $[1 \times 10 = 10]$

SECTION B

Followings are of 2 Marks each (Q11-12).

- Q11. Prove that : $\sqrt{\frac{\sec A 1}{\sec A + 1}} + \sqrt{\frac{\sec A + 1}{\sec A 1}} = 2 \csc A$.
- Q12. (a) If $\sin \alpha = \frac{1}{\sqrt{2}}$ and $\cot \beta = \sqrt{3}$, then find the value of $\csc \alpha + \csc \beta$.

OR

(b) Evaluate :
$$\frac{5\cos^2 60^\circ + 4\sec^2 30^\circ - \tan^2 45^\circ}{\sin^2 30^\circ + \sin^2 60^\circ}.$$

 $\lceil 2 \times 2 = 4 \rceil$

SECTION C

Followings are of 3 Marks each (Q13-16).

- Given that $(1 + \sin A)(1 + \sin B)(1 + \sin C) = (1 \sin A)(1 \sin B)(1 \sin C)$. Then prove that both are equal to $\pm \cos A \cos B \cos C$.
- (a) A rhombus of side 14 cm has two angles of 60° each. Find the length of the diagonals of the O14. rhombus.

- (b) If $\cos \theta + \cos^2 \theta = 1$, prove that $\sin^{12} \theta + 3\sin^{10} \theta + 3\sin^{8} \theta + \sin^{6} \theta + 2\sin^{4} \theta + 2\sin^{2} \theta 2 = 1$.
- If $\tan^2 \alpha = 1 + 2 \tan^2 \beta$, then prove that $2 \sin^2 \alpha = 1 + \sin^2 \beta$. O15.
- In an acute angled triangle ABC, if tan(A+B-C)=1 and sec(B+C-A)=2, then find the values of angles A, B and C.

 $[3 \times 4 = 12]$

SECTION D

Followings are of 5 Marks each (Q17-18).

- Q17. If $4\sin\theta = 3$, then find the value of x, if it is given that $\sqrt{\frac{\csc^2\theta \cot^2\theta}{\sec^2\theta 1}} + \cot\theta = \frac{\sqrt{7}}{x} + \cos\theta$.

 Q18. (a) If $\sec\theta = x + \frac{1}{x}$ prove that $\sec\theta + \tan\theta = 2$
- Q18. (a) If $\sec \theta = x + \frac{1}{4x}$, prove that $\sec \theta + \tan \theta = 2x$ or $\frac{1}{2x}$

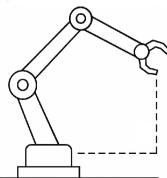
(b) If
$$\frac{\cos \alpha}{\cos \beta} = m$$
 and $\frac{\cos \alpha}{\sin \beta} = n$, then prove that $(m^2 + n^2)\cos^2 \beta = n^2$.

 $5\times 2=10$

SECTION E

Following is a case-study based question of 4 Marks (Q19); having three sub-parts (i), (ii) and (iii).

A software company is testing an AI-controlled robotic arm that rotates from a fixed base. The control system continuously measures the horizontal and vertical components of the arm's extension using trigonometric ratios.



If $\sin \theta + \cos \theta = \frac{5}{4}$, where θ is the angle made by arm with horizontal, then answer the following questions.

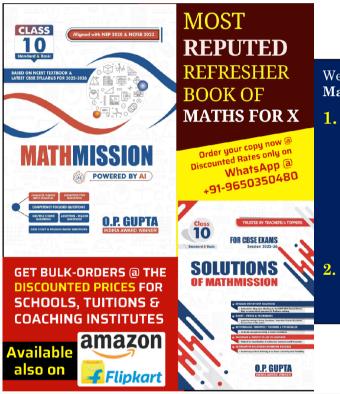
- Find the value of $\sin \theta \cos \theta$. (i)
- (ii) Find the value of $\cos \theta$.
- (a) Find the value of $\sin \theta$. Using values of $\sin \theta$ and $\cos \theta$ (as obtained in sub-part ii), show (iii) that $\sin^2 \theta + \cos^2 \theta = 1$.

OR

(b) If the arm makes an angle ϕ such that $\tan \phi = \frac{7}{24}$, find the value of $\frac{1 - \tan^2 \phi}{1 + \tan^2 \phi}$. Hence show that $\sec^2 \phi - \tan^2 \phi = 1$.

[1+1+2=4]

- © SHARE THIS FILE with all other math scholars.
- ① You may Add our mobile no. +919650350480 to your WhatsApp Groups for regular updates.
- ① MS Word files of MCQ Tests / Subjective Tests / Case-Study Questions are available for SALE.



We have released **Set of 2 Books** for **CBSE X** Maths (Standard & Basic) useful for 2025-26.

1. MATHMISSION FOR X

- ☑ COMPLETE THEORY & EXAMPLES ✓ SUBJECTIVE TYPE QUESTIONS ☑ COMPETENCY FOCUSED QUESTIONS
 - ♠ Multiple Choice Questions
 - ❖ Assertion-Reason Questions
 - Case-Study / Passage Based Questions
- ☑ Selected Questions from recent exams.
- ☑ Answers of all the Questions of Exercises

2. SOLUTIONS OF MATHMISSION

✓ Step-by-step Detailed Solutions (For all the Exercises of MATHMISSION)

Grab the best Seller book for X, XI & XII Maths (041) CBSE Exams.

☑ MATHMISSION FOR XII. XI & X

(Refresher Guide with Competency Focused Questions)

The books are developed as per CBSE Curriculum for 2025-26.

☑ CBSE 39 SAMPLE PAPERS FOR XII

☑ CBSE YODDHA SAMPLE PAPERS FOR XI

☑ CBSE UMANG SAMPLE PAPERS FOR X

(Order now at Discounted rate on WhatsApp - 9650350480)



™ ONLINE CLASSES NOW AVAILABLE

(For Classes X - XI - XII Mathematics)

To know more, WhatsApp @ 9650350480



MATHEMATICIA BY O.P. GUPTA

...a name you can bank upon!



Feel Safe to Share this Document with other math scholars

CLICK NOW

Download



or, just type theopgupta.com

FREE PDF TESTS AND **ASSIGNMENTS OF THE CLASSES XII, XI & X**



To get FREE PDF Materials, join **WhatsApp Teachers Group** by Clicking on the Logo

You can add our WhatsApp no. +919650350480 to your Groups also

Click on the **Book cover** to buv!



If you are a Student, then you may join our Students Group

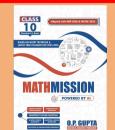


CLICK HERE FOR **CLASSES** XI & XII









Many Direct Questions from our Books have been asked in the recent CBSE Exams ATHMISSI

OR XII, XI & X

2025-26 Edition

Buy our books on







amazon **Flipkart**